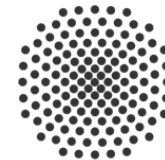


# *SIMPLE:* A Gradient Estimator for $k$ -Subset Sampling

Kareem Ahmed<sup>\*Δ</sup>, Zhe Zeng<sup>\*Δ</sup>, Mathias Niepert<sup>†</sup>, Guy Van den Broeck<sup>Δ</sup>

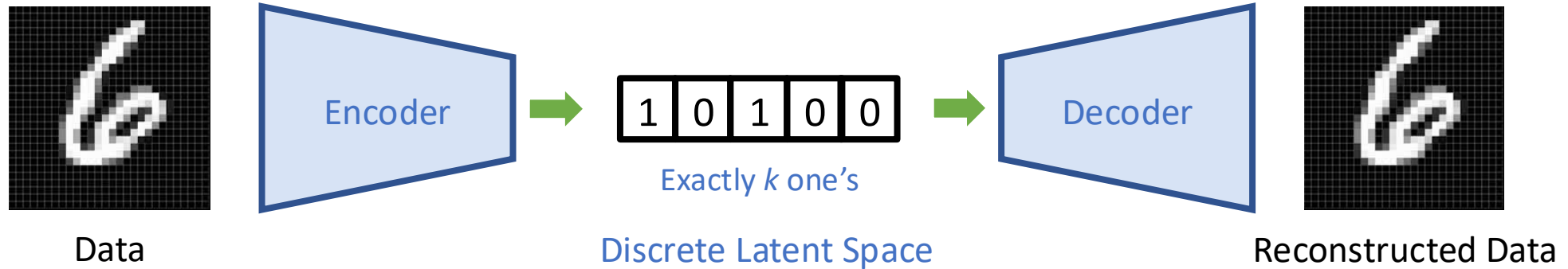
<sup>Δ</sup>UCLA <sup>†</sup>Stuttgart University



**University of  
Stuttgart**

# Why k-Subset Distributions?

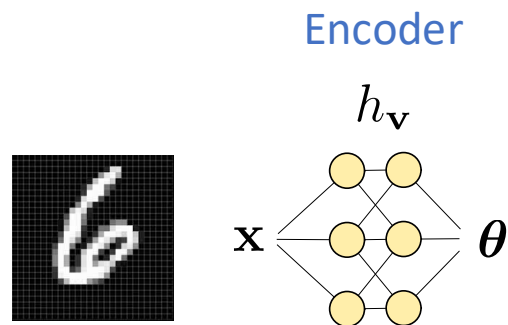
Example. Discrete VAE



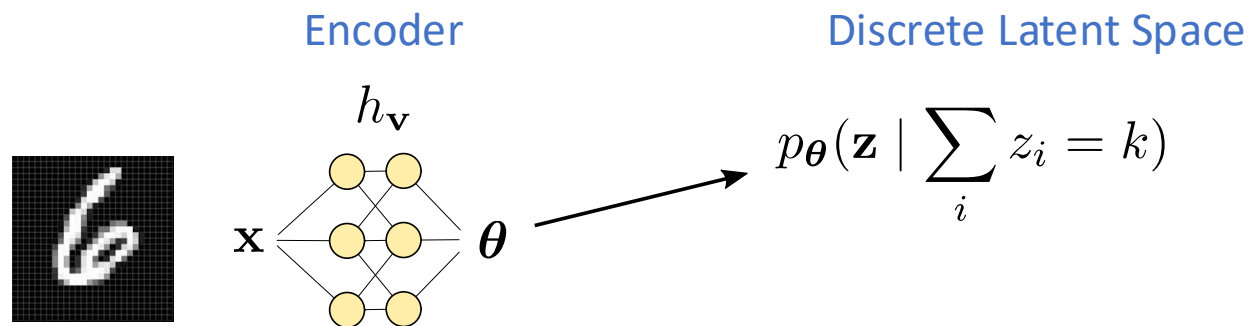
Example. Learn to Explain (L2X)

| Key Words ( $k = 10$ )                                                                                                                                                                                                                                                                                                     | Taste Score |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------|
| a lite bodied beer with a pleasant taste. was like a reddish color. a little like wood and caramel with a hop finish. has a sort of fruity flavor like grapes or cherry that is sort of buried in there. mouth feel was lite, sort of bubbly. not hard to down, though a bit harder then one would expect given the taste. | 0.7         |

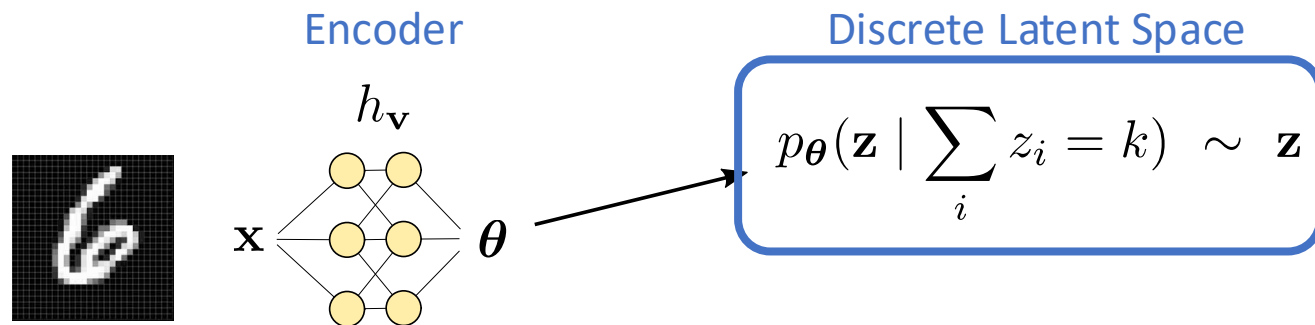
# *SIMPLE*: Gradient Estimator for $k$ -Subset Sampling



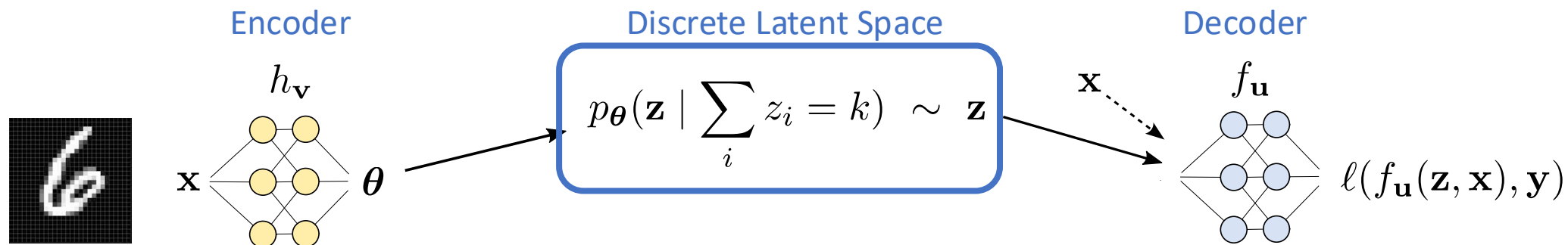
# *SIMPLE*: Gradient Estimator for $k$ -Subset Sampling



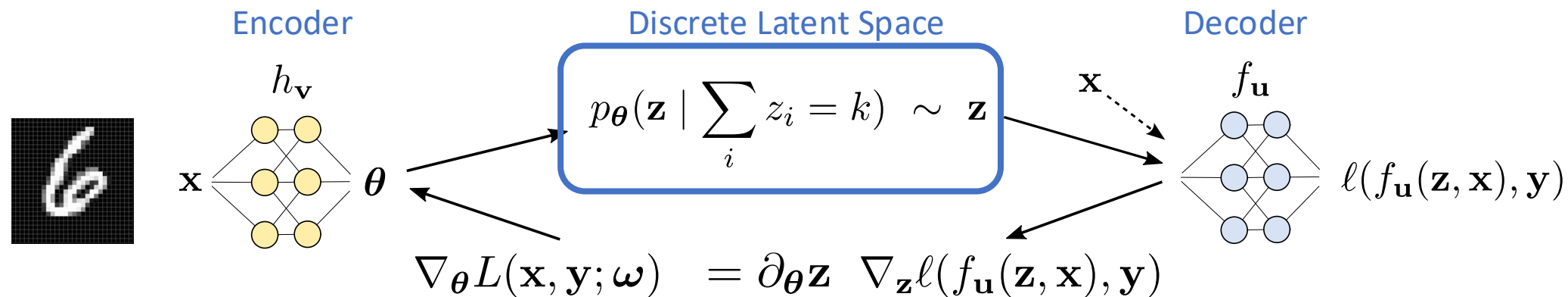
# *SIMPLE*: Gradient Estimator for $k$ -Subset Sampling



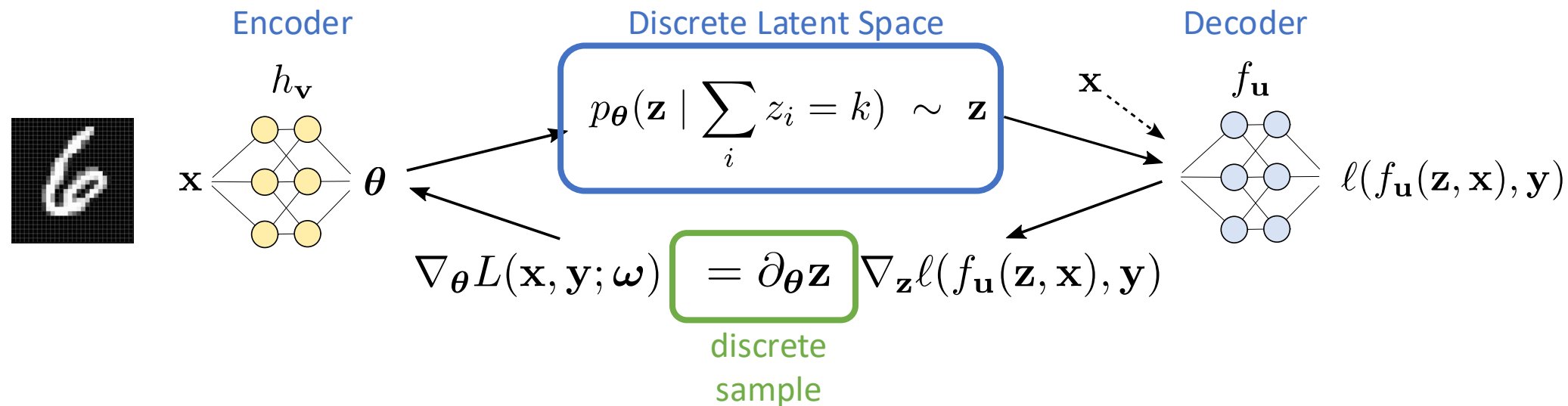
# *SIMPLE*: Gradient Estimator for $k$ -Subset Sampling



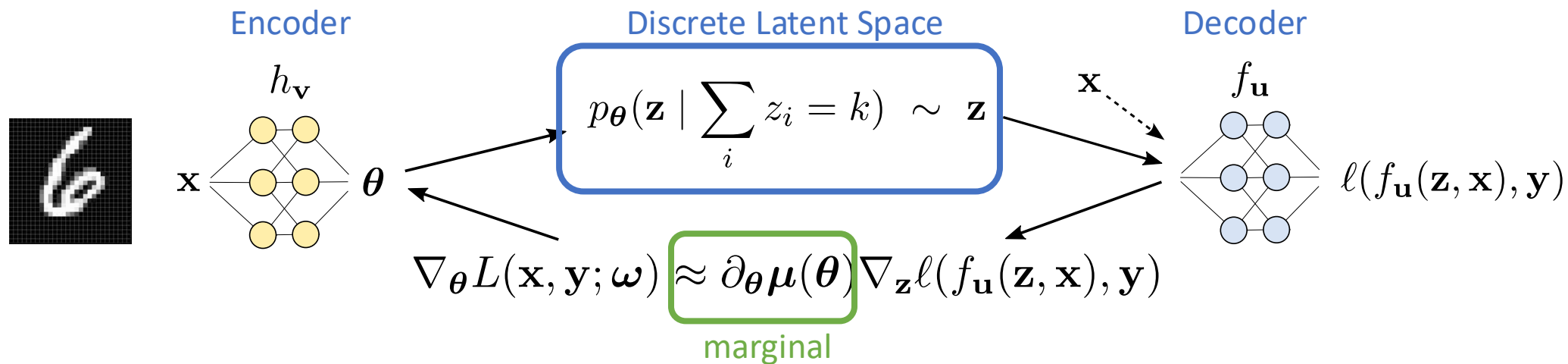
# *SIMPLE*: Gradient Estimator for $k$ -Subset Sampling



# *SIMPLE*: Gradient Estimator for $k$ -Subset Sampling

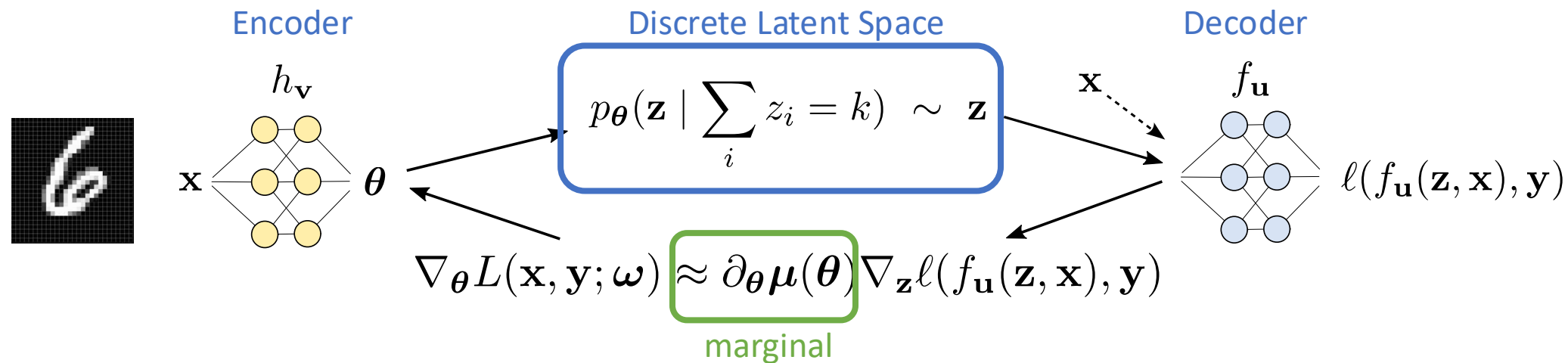


# *SIMPLE*: Gradient Estimator for $k$ -Subset Sampling

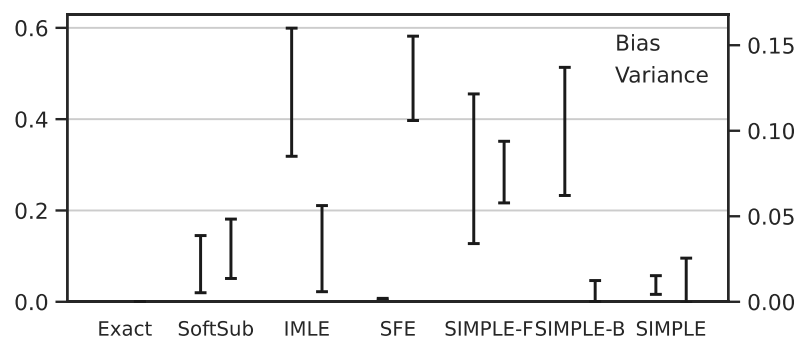


**Prop.** conditional marginals can be obtained by  $p_{\theta}(z_i \mid \sum_j z_j = k) = \frac{\partial}{\partial \theta_i} \log p_{\theta}(\sum_j z_j = k)$ .

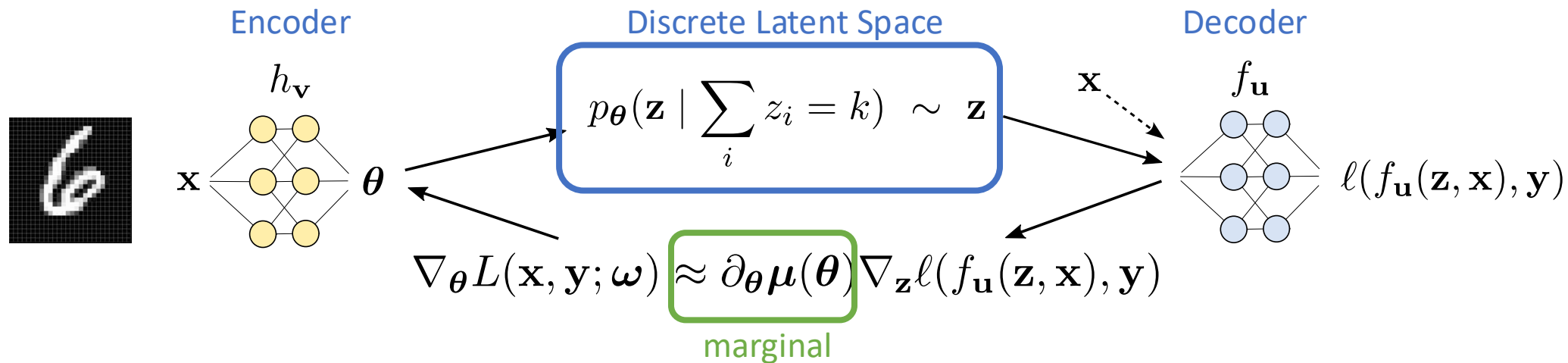
# *SIMPLE*: Gradient Estimator for $k$ -Subset Sampling



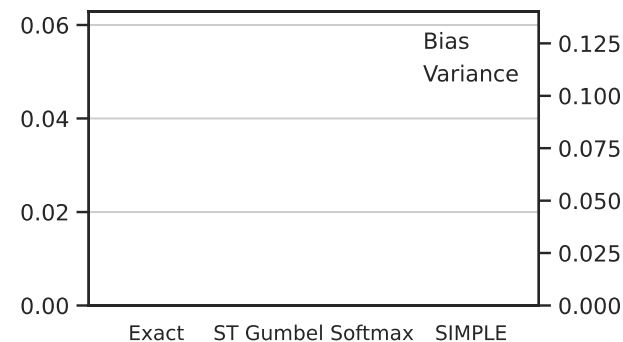
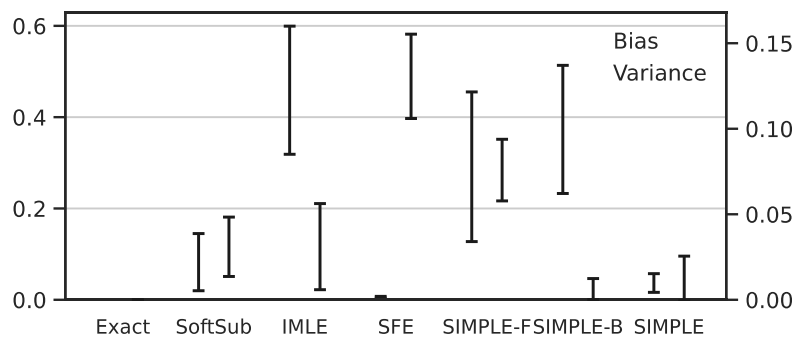
We achieve **lower bias and variance** by **exact, discrete samples** and **exact derivative of conditional marginals**.



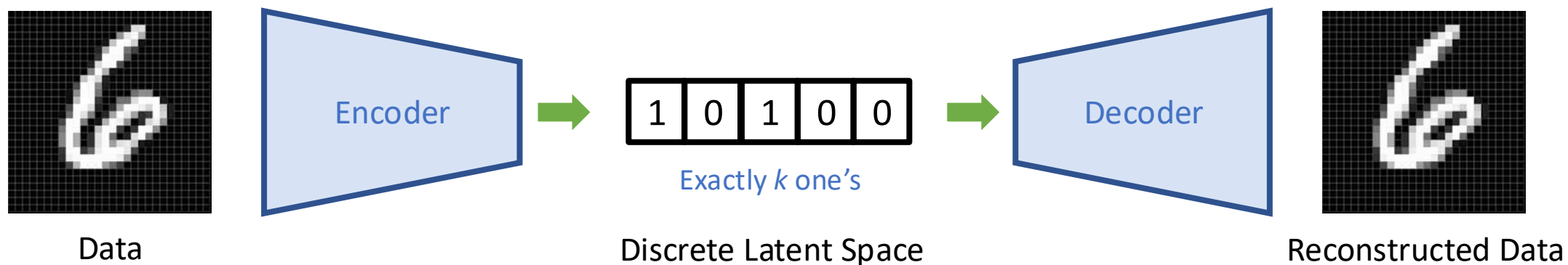
# *SIMPLE*: Gradient Estimator for $k$ -Subset Sampling



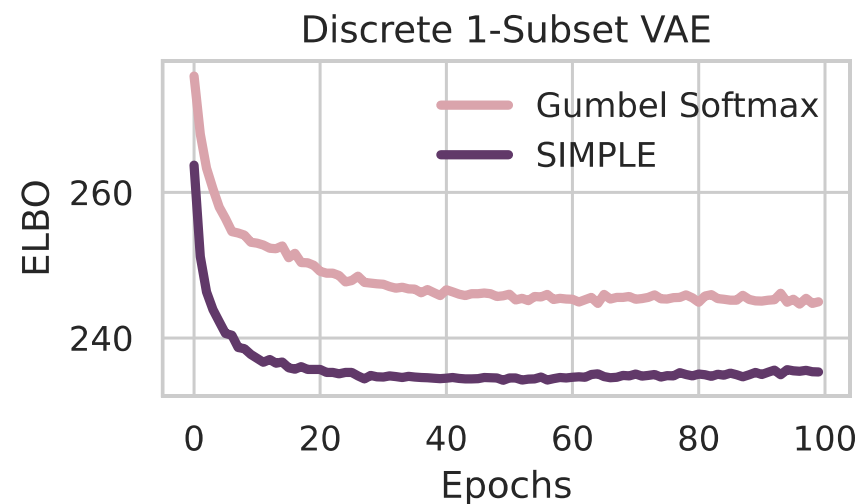
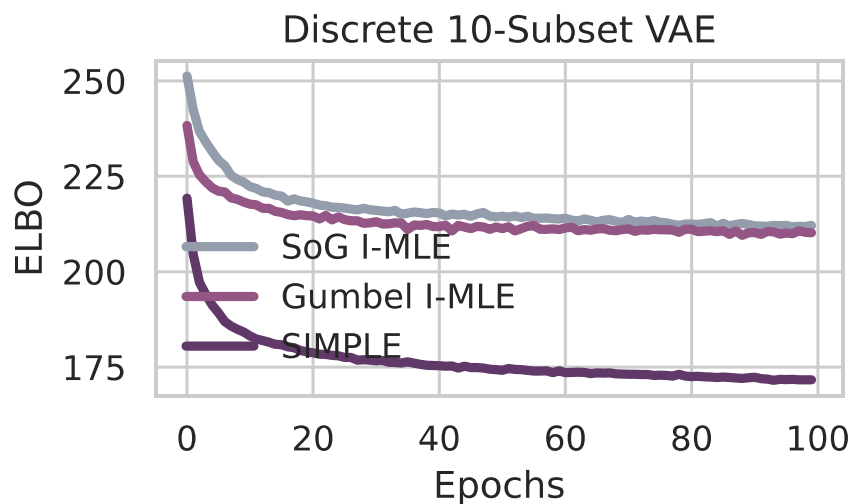
We achieve **lower bias and variance** by **exact, discrete samples** and **exact derivative of conditional marginals**.



# Experiment: Discrete VAE



## Metric: *exact* ELBO



# Experiment: Learn to Explain (L2X)

| Key Words ( $k = 10$ )                                                                                                                                                                                                                                                                                                     | Taste Score |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------|
| a lite bodied beer with a pleasant taste. was like a reddish color. a little like wood and caramel with a hop finish. has a sort of fruity flavor like grapes or cherry that is sort of buried in there. mouth feel was lite, sort of bubbly. not hard to down, though a bit harder then one would expect given the taste. | 0.7         |

Results for three aspects with  $k = 10$

| Method                | Appearance                        |                                    | Palate                            |                                     | Taste                             |                                    |
|-----------------------|-----------------------------------|------------------------------------|-----------------------------------|-------------------------------------|-----------------------------------|------------------------------------|
|                       | Test MSE                          | Precision                          | Test MSE                          | Precision                           | Test MSE                          | Precision                          |
| SIMPLE (Ours)         | <b>2.35 <math>\pm</math> 0.28</b> | <b>66.81 <math>\pm</math> 7.56</b> | <b>2.68 <math>\pm</math> 0.06</b> | <b>44.78 <math>\pm</math> 2.75</b>  | <b>2.11 <math>\pm</math> 0.02</b> | <b>42.31 <math>\pm</math> 0.61</b> |
| L2X ( $t = 0.1$ )     | 10.70 $\pm$ 4.82                  | 30.02 $\pm$ 15.82                  | 6.70 $\pm$ 0.63                   | <b>50.39 <math>\pm</math> 13.58</b> | 6.92 $\pm$ 1.61                   | 32.23 $\pm$ 4.92                   |
| SoftSub ( $t = 0.5$ ) | <b>2.48 <math>\pm</math> 0.10</b> | 52.86 $\pm$ 7.08                   | 2.94 $\pm$ 0.08                   | 39.17 $\pm$ 3.17                    | 2.18 $\pm$ 0.10                   | <b>41.98 <math>\pm</math> 1.42</b> |
| I-MLE ( $\tau = 30$ ) | <b>2.51 <math>\pm</math> 0.05</b> | <b>65.47 <math>\pm</math> 4.95</b> | 2.96 $\pm$ 0.04                   | 40.73 $\pm$ 3.15                    | 2.38 $\pm$ 0.04                   | <b>41.38 <math>\pm</math> 1.55</b> |

Results for aspect Aroma, for  $k$  in {5, 10, 15}

| Method                | $k = 5$                           |                                    | $k = 10$                          |                                    | $k = 15$                          |                                    |
|-----------------------|-----------------------------------|------------------------------------|-----------------------------------|------------------------------------|-----------------------------------|------------------------------------|
|                       | Test MSE                          | Precision                          | Test MSE                          | Precision                          | Test MSE                          | Precision                          |
| SIMPLE (Ours)         | <b>2.27 <math>\pm</math> 0.05</b> | <b>57.30 <math>\pm</math> 3.04</b> | <b>2.23 <math>\pm</math> 0.03</b> | <b>47.17 <math>\pm</math> 2.11</b> | 3.20 $\pm$ 0.04                   | <b>53.18 <math>\pm</math> 1.09</b> |
| L2X ( $t = 0.1$ )     | 5.75 $\pm$ 0.30                   | 33.63 $\pm$ 6.91                   | 6.68 $\pm$ 1.08                   | 26.65 $\pm$ 9.39                   | 7.71 $\pm$ 0.64                   | 23.49 $\pm$ 10.93                  |
| SoftSub ( $t = 0.5$ ) | 2.57 $\pm$ 0.12                   | <b>54.06 <math>\pm</math> 6.29</b> | 2.67 $\pm$ 0.14                   | 44.44 $\pm$ 2.27                   | <b>2.52 <math>\pm</math> 0.07</b> | 37.78 $\pm$ 1.71                   |
| I-MLE ( $\tau = 30$ ) | 2.62 $\pm$ 0.05                   | <b>54.76 <math>\pm</math> 2.50</b> | 2.71 $\pm$ 0.10                   | <b>47.98 <math>\pm</math> 2.26</b> | 2.91 $\pm$ 0.18                   | 39.56 $\pm$ 2.07                   |

*Thanks!*

- code: [github.com/UCLA-StarAI/SIMPLE](https://github.com/UCLA-StarAI/SIMPLE)